

CHAPTER TWELVE

GRAPHS:

Some basic graphs:

Before a graph can be plotted, we must first construct a table with reference to the equation of the given graph.

- A few values of x are selected and for each, the corresponding y value is computed.
- These two corresponding values i.e. the x and the y values are then plotted on a graph paper.
- There are certain basic graphs which students must be familiar with and be capable of plotting.
- The way or manner of plotting some of these graphs will be illustrated in the following questions:

Q1). Using values of x from -2 to 2, plot the following graphs:

1) $y = 2x$. 2) $y + 4x = 0$.

3) $y = \frac{1}{2}x$. 4) $y = -\frac{x}{2}$.

5) $y = 2x + 1$. 6) $y + 4x + 2 = 0$.

Soln.

(1) $y = 2x$

| | | | | | |
|---|-----|-----|---|---|---|
| X | - 2 | - 1 | 0 | 1 | 2 |
| Y | - 4 | - 2 | 0 | 2 | 4 |

(a) If $x = -2$

$$\begin{aligned}y &= 2x \\ \Rightarrow y &= 2(-2) = -4 \\ \Rightarrow y &= -4\end{aligned}$$

(b) If $x = -1$

$$\begin{aligned}y &= 2x \\ \Rightarrow y &= 2(-1) \\ \Rightarrow y &= -2\end{aligned}$$

© If $x = 0$

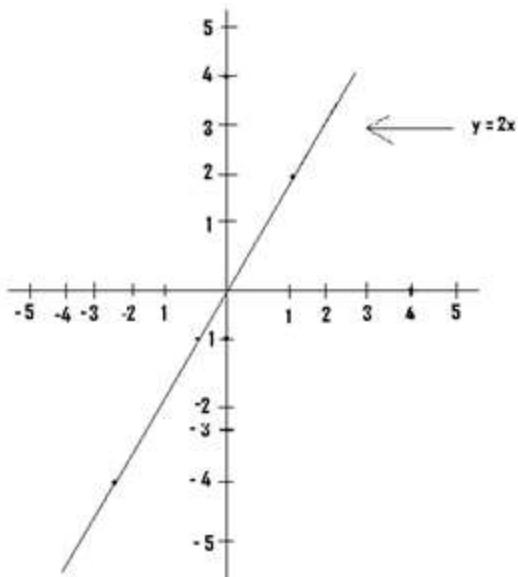
$$\begin{aligned}y &= 2x \\ \Rightarrow y &= 2(0) = 0 \\ \Rightarrow y &= 0\end{aligned}$$

(d) If $x = 1$

$$\begin{aligned}y &= 2x \\ \Rightarrow y &= 2(1) = 2 \\ \Rightarrow y &= 2\end{aligned}$$

(e) If $x = 2$

$$\begin{aligned}y &= 2x \\ \Rightarrow y &= 2(2) \\ \Rightarrow y &= 4\end{aligned}$$



N/B: Before plotting any graph you, must first make sure y is the subject of the given equation. If not, then make y the subject.

(2) From $y + 4x = 0$, $\Rightarrow y = 0 - 4x \Rightarrow y = -4x$

$$y = -4x$$

| | | | | | |
|---|----|----|---|----|----|
| X | -2 | -1 | 0 | 1 | 2 |
| Y | 8 | 4 | 0 | -4 | -8 |

(a) If $x = -2$

$$\begin{aligned} y &= -4x \\ \Rightarrow y &= -4(-2) \\ \Rightarrow y &= 8 \end{aligned}$$

(b) If $x = -1$

$$\begin{aligned} \Rightarrow y &= -4(-1) \\ \Rightarrow y &= 4 \end{aligned}$$

(c) If $x = 0$

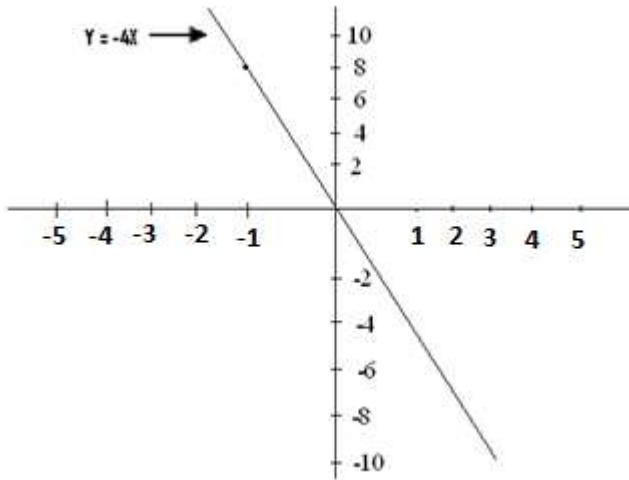
$$\begin{aligned} y &= -4x \\ \Rightarrow y &= -4(0) \\ \Rightarrow y &= 0 \end{aligned}$$

(d) If $x = 1$

$$\begin{aligned} y &= -4x \\ \Rightarrow y &= -4(1) = -4 \\ \Rightarrow y &= -4 \end{aligned}$$

(e) If $x = 2$

$$\begin{aligned} y &= -4x \\ \Rightarrow y &= -4(2) = -8 \\ \Rightarrow y &= -8 \end{aligned}$$



1. $y = \frac{1x}{2}$ { or $y = x/2$ }

3) $y = \frac{x}{2}$ or $y = \frac{1x}{2}$

| | | | | | |
|---|----|------|---|-----|---|
| X | -2 | -1 | 0 | 1 | 2 |
| Y | -1 | -0.5 | 0 | 0.5 | 1 |

(a) If $x = -2$

$$y = \frac{1x}{2} = \frac{1}{2}(-2)$$

$$\Rightarrow y = -2/2$$

$$\therefore y = -1$$

(b) If $x = -1$

$$y = \frac{1x}{2} = \frac{1}{2}(-1)$$

$$\Rightarrow y = -1/2 = -0.5$$

$$\therefore y = -0.5$$

(c) If $x = 0$

$$y = \frac{1x}{2} = \frac{1}{2}(0)$$

$$\Rightarrow y = 0/2$$

$$\therefore y = 0$$

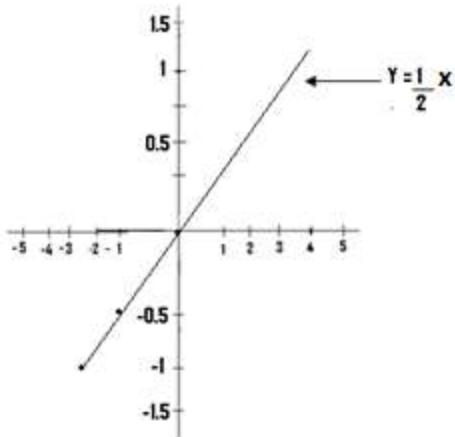
(d) If $x = 1$

$$y = \frac{1x}{2} = \frac{1}{2}(1)$$

$$\Rightarrow y = 1/2$$

$$\therefore y = 0.5$$

| | | | | | |
|---|----|-----|---|------|----|
| X | -2 | -1 | 0 | 1 | 2 |
| Y | 1 | 0.5 | 0 | -0.5 | -1 |



N/B: In the plotting of a graph, the interval used on one particular axis (i.e. the difference between one number and the next) must be the same.

- For a particular graph, the interval used on the x-axis must be the same.
- But the scale used on the x-axis can be different from that used on the y-axis.

4) $y = -x/2$. or $y = \frac{-x}{2}$

1) If $x = -2$

$$y = -x/2 = -(-2)/2$$

$$\Rightarrow y = 2/2 = 1$$

2) If $x = -1$

$$y = -x/2 = -(-1)/2$$

$$\Rightarrow y = 1/2 = 0.5$$

3) If $x = 0$

4) If $x = 1$

$$y = -x/2 = -(0)/2 = 0$$

$$\Rightarrow y = 0.$$

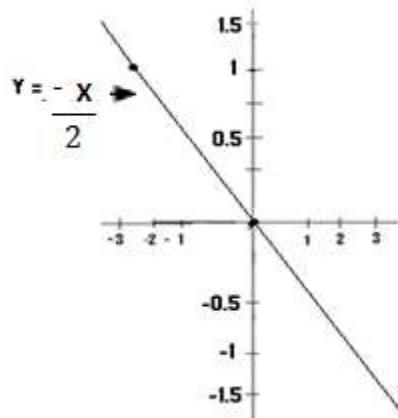
$$y = -x/2 = -(1)/2$$

$$\Rightarrow y = -1/2 = -0.5$$

5) If $x = 2$

$$y = -x/2 = -(2)/2$$

$$\Rightarrow y = -1$$



5)

$$y = 2x + 1$$

| | | | | | |
|---|----|----|---|---|---|
| X | -2 | -1 | 0 | 1 | 2 |
| Y | -3 | -1 | 1 | 3 | 5 |

1) If $x = -2$

$$y = 2x + 1$$

$$\Rightarrow y = 2(-2) + 1$$

$$\Rightarrow y = -4 + 1 = -3.$$

2) If $x = -1$

$$y = 2x + 1$$

$$\Rightarrow y = 2(-1) + 1 = -2 + 1$$

$$\Rightarrow y = -1.$$

3) If $x = 0$

$$y = 2x + 1$$

$$\Rightarrow y = 2(0) + 1$$

$$\Rightarrow y = 0 + 1 = 1.$$

4) If $x = 1$

$$y = 2x + 1$$

$$\Rightarrow y = 2(1) + 1 = 2 + 1 = 3$$

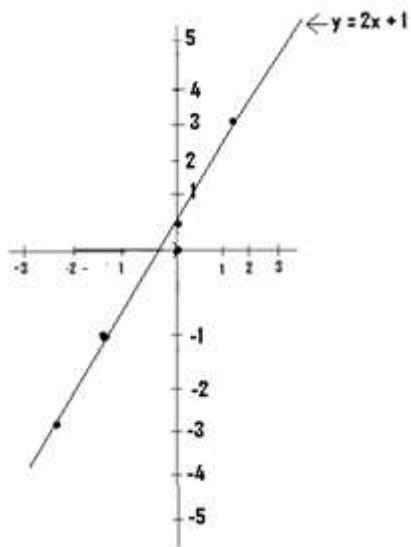
$$\Rightarrow y = 3.$$

5) If $x = 2$

$$y = 2x + 1$$

$$\Rightarrow y = 2(2) + 1$$

$$\Rightarrow y = 5.$$



6) From $y + 4x + 2 = 0$

$$\Rightarrow y + 2 = 0 - 4x$$

$$\Rightarrow y + 2 = -4x$$

$$\Rightarrow y = -4x - 2$$

$$y = -4x - 2$$

| | | | | | |
|---|----|----|----|----|-----|
| X | -2 | -1 | 0 | 1 | 2 |
| Y | 6 | 2 | -2 | -6 | -10 |

a) If $x = -2$

$$y = -4x - 2$$

$$\Rightarrow y = -4(-2) - 2$$

$$\Rightarrow y = 8 - 2$$

$$\Rightarrow y = 6$$

b) If $x = -1$

$$y = -4x - 2$$

$$\Rightarrow y = -4(-1) - 2$$

$$\Rightarrow y = 4 - 2$$

$$\Rightarrow y = 2$$

c) If $x = 0$

$$y = -4x - 2$$

$$\Rightarrow y = -4(0) - 2$$

$$\Rightarrow y = 0 - 2 = -2.$$

d) If $x = 1$

$$y = -4x - 2$$

$$\Rightarrow y = -4(1) - 2$$

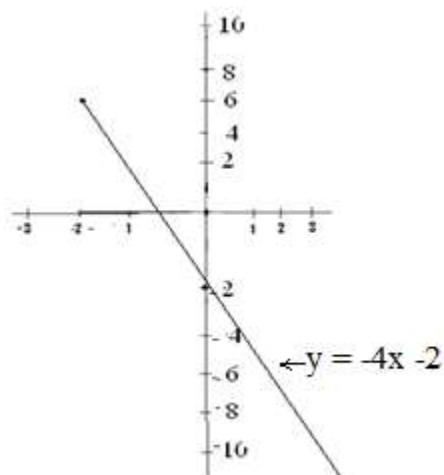
$$\Rightarrow y = -4 - 2 = -6.$$

If $x = 2$

$$y = -4x - 2$$

$$\Rightarrow y = -4(2) - 2 = .$$

$$-8 - 2 = -10.$$



Q2) Using values of x from -3 to 3, plot the graphs of the relations: a) $y = x^2$.

b) $y = -x^2$

c) $y = 2x^2$

d) $y + 2x^2 = 0$

e) $y = \frac{1}{2}x^2$

Soln

a) $y = x^2$

$$y = x^2$$

| | | | | | | | |
|---|----|----|----|---|---|---|---|
| X | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| Y | 9 | 4 | 1 | 0 | 1 | 4 | 9 |

(1) If $x = -3$

$$y = x^2$$

$$\Rightarrow y = (-3)^2 = 9.$$

$$\Rightarrow y = 9.$$

2) If $x = -2$

$$y = x^2$$

$$\Rightarrow y = (-2)^2 = 4.$$

$$\Rightarrow y = 4.$$